

## PC #2 Review WS - Unit 6 Factoring

Factor the GCF out of each expression.

1)  $-2b^2 + b^3$

$b^2(b-2)$

2)  $-9n + 6$

$-3(3n-2)$

3)  $-16b^3 - 8b^2 + 12b$

$-4b(4b^2 + 2b - 3)$

4)  $6x^2 + 8x + 4$

$2(3x^2 + 4x + 2)$

Factor each completely.

$$\begin{array}{|c|c|c|c|} \hline 54 & & & \\ \hline 1 & 54 & & \\ \hline 2 & 27 & & \\ \hline 3 & 18 & & \\ \hline 6 & 9 & & \\ \hline \end{array}$$

5)  $a^2 + 15a + 54$

$$(a^2 + \cancel{6a}) + (9a + 54)$$

$$a(a+6) + 9(a+6)$$

$(a+9)(a+6)$

$$\begin{array}{|c|c|} \hline a & 6 \\ \hline a^2 & 6a \\ \hline 9a & 54 \\ \hline \end{array}$$

$$(a+6)(a+9)$$

6)  $x^2 - 3x - 10$

$$(x^2 + \cancel{2x}) - (5x - 10)$$

$$x(x+2) - 5(x+2)$$

$(x-5)(x+2)$

$$\begin{array}{|c|c|} \hline x & 2 \\ \hline x^2 & 2x \\ \hline -5x & -10 \\ \hline \end{array}$$

$$(x+2)(x-5)$$

$$\begin{array}{|c|c|c|c|} \hline 72 & & & \\ \hline 1 & 72 & & \\ \hline 2 & 36 & & \\ \hline 3 & 24 & & \\ \hline 4 & 18 & & \\ \hline 6 & 12 & & \\ \hline 8 & 9 & & \\ \hline \end{array}$$

7)  $x^2 + 17x + 72$

$$(x^2 + \cancel{8x}) + (9x + 72)$$

$$x(x+8) + 9(x+8)$$

$(x+9)(x+8)$

$$\begin{array}{|c|c|} \hline x & 8 \\ \hline x^2 & 8x \\ \hline 9x & 72 \\ \hline \end{array}$$

$$(x+9)(x+8)$$

8)  $m^2 - 3m - 18$

$$(m^2 + \cancel{3m}) - (6m - 18)$$

$$m(m+3) - 6(m+3)$$

$(m-6)(m+3)$

$$\begin{array}{|c|c|} \hline m & 3 \\ \hline m^2 & 3m \\ \hline -6m & -18 \\ \hline \end{array}$$

$$(m-6)(m+3)$$

$$\begin{array}{|c|c|c|c|} \hline -60 & & & \\ \hline 1 & 40 & & \\ \hline 2 & 30 & & \\ \hline 3 & 20 & & \\ \hline 4 & 15 & & \\ \hline 5 & 12 & & \\ \hline 6 & 10 & & \\ \hline \end{array}$$

9)  $3x^2 + 11x - 20$

$$(3x^2 - \cancel{4x}) + (15x - 20)$$

$$x(3x-4) + 5(3x-4)$$

$(3x-4)(x+5)$

$$\begin{array}{|c|c|} \hline x & -4 \\ \hline 3x^2 & -4x \\ \hline 15x & -20 \\ \hline \end{array}$$

$$(3x-4)(x+5)$$

10)  $3a^2 - a - 2$

$$(3a^2 + \cancel{2a}) - (3a + 2)$$

$$a(3a+2) - 1(3a+2)$$

$(a-1)(3a+2)$

$$\begin{array}{|c|c|} \hline 3a & 2 \\ \hline 3a^2 & 2a \\ \hline -3a & -2 \\ \hline \end{array}$$

$$(a-1)(3a+2)$$

$$\begin{array}{|c|c|c|c|} \hline 10 & & & \\ \hline 1 & 10 & & \\ \hline 2 & 5 & & \\ \hline \end{array}$$

11)  $2n^2 + 11n + 5$

$$(2n^2 + \cancel{n}) + (10n + 5)$$

$$n(2n+1) + 5(2n+1)$$

$(n+5)(2n+1)$

$$\begin{array}{|c|c|} \hline 2n & 1 \\ \hline 2n^2 & 1n \\ \hline 10n & 5 \\ \hline \end{array}$$

$$(2n+1)(n+5)$$

12)  $42r^2 + 204r + 144$

$$GCF = 6$$

$$6(7r^2 + 34r + 24)$$

$$(7r^2 + \cancel{6r})(28r + 24)$$

$$r(7r+6) + 4(7r+6)$$

$6(r+6)(7r+6)$

$$\begin{array}{|c|c|} \hline 7r & 6 \\ \hline 7r^2 & 6r \\ \hline 28r & 24 \\ \hline \end{array}$$

$6(r+6)(7r+6)$

$$\begin{array}{r} -400 \\ \hline -20 | 20 \end{array} \quad 13) 16k^2 - 25$$

$$(16k^2 - 20k)(20k - 25)$$

$$4k(4k-5) + 5(4k-5)$$

$$(4k+5)(4k-5)$$

$$\begin{array}{c} 4k \quad 5 \\ \hline 4k & (16k^2 \quad 20k) \\ -5 & -20k \quad -25 \end{array}$$

$$(4k+5)(4k-5)$$

$$-4 \quad 14) p^2 - 4$$

$$-2 \quad p^2 + 0p - 4$$

$$(p^2 - 2p) + 2(p - 4)$$

$$p(p-2) + 2(p-4)$$

$$\frac{(p+2)(p-2)}{(p+2)(p-2)}$$

$$\begin{array}{c} p \quad -2 \\ \hline p & (p^2 \quad -2p) \\ 2 & 2p \quad -4 \end{array}$$

$$(p-2)(p+2)$$

$$\begin{array}{c} 36 \\ \hline 1 \quad 36 \\ 2 \quad 18 \\ 3 \quad 12 \\ 4 \quad 9 \\ 5 \quad 6 \end{array} \quad 15) 4n^2 + 12n + 9$$

$$(4n^2 + 6n) + (6n + 9)$$

$$2n(2n+3) + 3(2n+3)$$

$$(2n+3)(2n+3)$$

$$\frac{(2n+3)^2}{(2n+3)^2}$$

$$\begin{array}{c} 2n \quad 3 \\ \hline 2n & (4n^2 \quad 6n) \\ 3 & 6n \quad 9 \end{array}$$

$$(2n+3)^2$$

$$17) (7x^3 - 2x^2)(-49x + 14)$$

$$x^2(7x-2) - 7(7x-2)$$

$$\boxed{(x^2-7)(7x-2)}$$

$$\begin{array}{c} 7x \quad -2 \\ \hline x^2 & (7x^3 \quad -2x^2) \\ -7 & -49x \quad 14 \end{array}$$

$$(7x-2)(x^2-7)$$

$$19) (2a^3 + 3a^2) + (16a + 24)$$

$$a^2(2a+3) + 8(2a+3)$$

$$\boxed{(a^2+8)(2a+3)}$$

$$\begin{array}{c} 2a \quad 3 \\ \hline a^2 & (2a^3 \quad 3a^2) \\ 8 & 16a \quad 24 \end{array}$$

$$(2a+3)(a^2+8)$$

$$16) 16r^2 + 24r + 9$$

$$(4r^2 + 12r) + (12r + 9)$$

$$4r(4r+3) + 3(4r+3)$$

$$\begin{array}{c} 4r \quad 3 \\ \hline 4r & (16r^2 \quad 12r) \\ 3 & 12r \quad 9 \end{array}$$

$$(4r+3)^2$$

$$18) (4r^3 - 14r^2)(-6r + 21)$$

$$2r^2(2r-7) - 3(2r-7)$$

$$(2r^2-3)(2r-7)$$

$$\begin{array}{c} 2r \quad -7 \\ \hline 2r^2 & (4r^3 \quad -14r^2) \\ -3 & -6r \quad 21 \end{array}$$

$$(2r-7)(2r^2-3)$$

$$20) (x^3 - 3x^2) + (3x - 9)$$

$$x^2(x-3) + 3(x-3)$$

$$(x^2+3)(x-3)$$

$$\begin{array}{c} x \quad -3 \\ \hline x^2 & (x^3 \quad -3x^2) \\ 3 & 3x \quad -9 \end{array}$$

$$(x^2+3)(x-3)$$

Solve each equation by factoring.

$$-42 \quad 21) x^2 + x - 42 = 0$$

$$\boxed{x = -7, 6}$$

$$(x^2 - 6x)(7x - 42) = 0$$

$$x(x-6) + 7(x-6) = 0$$

$$(x+7)(x-6) = 0$$

$$x = -7 \quad x+7 = 0 \quad x-6 = 0 \quad \boxed{x=6}$$

$$-42 \quad 23) 7a^2 - 11a - 2 = 0$$

$$\boxed{a = 2, -\frac{3}{7}}$$

$$(7a^2 + 3a)(-14a - 4) = 0$$

$$a(7a+3) - 2(7a+3) = 0$$

$$(a-2)(7a+3) = 0$$

$$a-2 = 0 \quad 7a+3 = 0$$

$$\frac{+2 \quad +2}{a=2} \quad \frac{-2 \quad -3}{7a=-3}$$

$$a = 2 \quad a = -\frac{3}{7}$$

$$22) 3m^2 + 14m - 42 = 0$$

$$\boxed{m = -7, \frac{7}{3}}$$

$$(3m^2 + 7m)(21m - 49) = 0$$

$$m(3m-7) + 7(3m-7) = 0$$

$$(m+7)(3m-7) = 0$$

$$\begin{array}{c} 3m \quad -7 \\ \hline m & (3m^2 \quad -7m) \\ 7 & 21m \quad -49 \end{array}$$

$$24) n^2 - 4n - 15 = 0$$

$$\boxed{n = -7, 3}$$

$$(n^2 + 3n)(-7n - 21) = 0$$

$$n(n+3) - 7(n+3) = 0$$

$$(n-7)(n+3) = 0$$

$$\begin{array}{c} n \quad 3 \\ \hline n & (n^2 \quad 3n) \\ -7 & -7n \quad -21 \end{array}$$

$$n-7 = 0 \quad n+3 = 0$$

$$\frac{+7 \quad +7}{n=7} \quad \frac{-3 \quad -3}{n=-3}$$