

Name:

Date:

Hour:

KEY

Algebra 1
Unit 1 Review

Simplify each radical expression.

1. $-2\sqrt{24}$

$$\begin{array}{c} \swarrow \quad \searrow \\ \sqrt{2} \quad \sqrt{2} \quad \sqrt{2} \quad \sqrt{3} \\ \hline -2 \cdot 2\sqrt{6} \\ \hline -4\sqrt{6} \end{array}$$

2. $6\sqrt{54}$

$$\begin{array}{c} \swarrow \quad \searrow \\ \sqrt{3} \quad \sqrt{3} \quad \sqrt{3} \quad \sqrt{2} \\ \hline 6 \cdot 3\sqrt{6} \\ \hline 18\sqrt{6} \end{array}$$

3. $\sqrt{72}$

$$\begin{array}{c} \swarrow \quad \searrow \\ \sqrt{3} \quad \sqrt{3} \quad \sqrt{2} \quad \sqrt{2} \\ \hline 3 \cdot 2\sqrt{2} \\ \hline 6\sqrt{2} \end{array}$$

4. Solve for x: $4(x-2) + 6x = 12 + 5x$.

$$4x - 8 + 6x = 12 + 5x$$

$$\begin{array}{r} 10x - 8 = 12 + 5x \\ -5x \quad -5x \\ \hline 5x - 8 = 12 \\ +8 \quad +8 \\ \hline 5x = 20 \end{array}$$

$$\frac{5x}{5} = \frac{20}{5}$$

$$x = 4$$

5. Write and solve an equation to represent the following:

The difference of twice a number and 4 is 8

$$2x - 4 = 8$$

$$\begin{array}{r} 2x - 4 = 8 \\ +4 \quad +4 \\ \hline 2x = 12 \\ \hline \frac{2x}{2} = \frac{12}{2} \end{array}$$

$$x = 6$$

Solve each equation.

6. $3(2x-5) = 2(3x-2)$

$$\begin{array}{r} 6x - 15 = 6x - 4 \\ -6x \quad -6x \\ \hline -15 = -4 \end{array}$$

No solution

7. $4x - 3 = 2x + 5$

$$\begin{array}{r} 4x - 3 = 2x + 5 \\ -2x \quad -2x \\ \hline 2x - 3 = 5 \\ +3 \quad +3 \\ \hline 2x = 8 \end{array}$$

$$\frac{2x}{2} = \frac{8}{2}$$

$$x = 4$$

8. $\frac{15}{3}x - \frac{6(15)}{1(15)} = \frac{4(3)}{5(3)}$

$$\frac{10}{15}x - \frac{90}{15} = \frac{12}{15}$$

$$\begin{array}{r} 10x - 90 = 12 \\ +90 \quad +90 \\ \hline 10x = 102 \end{array}$$

$$\frac{10x}{10} = \frac{102}{10}$$

$$x = \frac{102}{10} = \frac{51 \cdot 2}{5 \cdot 2}$$

$$x = \frac{51}{5}$$

9. On the first day of the year, Alicia has \$1000 in her savings account and started spending \$25 a week. Her sister Kelsey had \$650 in her savings account and started saving \$15 a week. After how many weeks will the sisters have the same amount? What will that amount be?

$x = \text{weeks}$

$$1000 - 25x = 650 + 15x$$

$$\begin{array}{r} 1000 \\ - 650 \\ \hline 350 = 40x \end{array}$$

$$\frac{350}{40} = \frac{40x}{40}$$

$$x = 8.75 \text{ weeks}$$

10. Solve the equation. Write a justification for each step.

Statements	Reasons
$25 = 5(x - 3)$	Given
$25 = 5x - 15$	Dist. POE
$\begin{array}{r} +15 \\ \hline 40 = 5x \end{array}$	Add. POE
$\frac{40}{5} = \frac{5x}{5}$	Simplify
$8 = x$	Div. POE
$x = 8$	Simplify
	Symmetric POE

$$1000 - 25x$$

$$= 1000 - 25(8.75)$$

$$= 1000 - 218.75$$

$$= \$781.25$$

Solve each inequality. Then graph.

11. $-125 \geq 8p - 5$

$$\begin{array}{r} +5 \\ \hline -120 \geq 8p \\ \hline -15 \geq p \end{array}$$

$p \leq -15$

12. $9 + \frac{x}{3} > 13$

$$\begin{array}{r} -9 \\ \hline 3 \left(\frac{x}{3} \right) > (4) \cdot 3 \\ \hline x > 12 \end{array}$$

13. $98 < 7(3x + 5)$

$$\begin{array}{r} 98 < 21x + 35 \\ -35 \\ \hline 63 < 21x \\ \hline 3 < x \\ \hline x > 3 \end{array}$$

14. $-5(n + 1) - 6n \leq 83$

$$\begin{array}{r} -5n - 5 - 6n \leq 83 \\ -11n - 5 \leq 83 \\ +5 \\ \hline -11n \leq 88 \\ \hline n \geq -8 \end{array}$$

15. $6x - 5(8 - 5x) < 16 + 3x$

$$\begin{array}{r} 6x - 40 + 25x < 16 + 3x \\ 31x - 40 < 16 + 3x \\ -3x \\ \hline 28x - 40 < 16 \\ +40 \\ \hline 28x < 56 \\ \hline x < 2 \end{array}$$

16. $3(x + 1) \geq 2(-2 + x)$

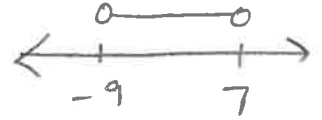
$$\begin{array}{r} 3x + 3 \geq -4 + 2x \\ -2x \\ \hline 1x + 3 \geq -4 \\ -3 \\ \hline x \geq -7 \end{array}$$

Solve each compound inequality and graph its solution.

$$\begin{array}{r}
 17. \quad 33 > -8x - 7 \geq -79 \\
 +7 \quad +7 \quad +7 \\
 \hline
 40 > -8x \geq -72 \\
 -8 \quad -8 \quad -8 \\
 \hline
 -5 < x \leq 9
 \end{array}$$



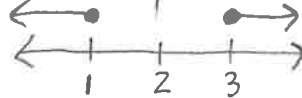
$$\begin{array}{r}
 18. \quad -15 < -3(x-2) < 33 \\
 -15 < -3x+6 < 33 \\
 -6 \quad -6 \quad -6 \\
 \hline
 -21 < -3x < 27 \\
 -3 \quad -3 \quad -3 \\
 \hline
 7 > x > -9 \\
 -9 < x < 7
 \end{array}$$



$$\begin{array}{r}
 19. \quad -7x+7 > 42 \text{ or } 2-x \leq -2 \\
 -7 \quad -7 \quad -2 \quad -2 \\
 \hline
 -7x > 35 \quad \quad x \leq -4 \\
 -7 \quad -7 \quad -x \quad -1 \\
 \hline
 x < -5 \text{ or } x \geq 4
 \end{array}$$



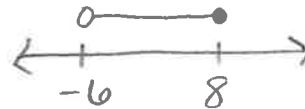
$$\begin{array}{r}
 20. \quad 8x-4 \geq 20 \text{ or } 5x-1 \leq 4 \\
 +4 \quad +4 \quad +1 \quad +1 \\
 \hline
 8x \geq 24 \quad \quad 5x \leq 5 \\
 8 \quad 8 \quad 5 \quad 5 \\
 \hline
 x \geq 3 \text{ or } x \leq 1
 \end{array}$$



21. A number x is more than -6 and at most 8 . Write this sentence as an inequality. Graph the solutions.

$$\begin{array}{l}
 x > -6 \quad \leq 8 \\
 x > -6 \quad x \leq 8
 \end{array}$$

$$\boxed{-6 < x \leq 8}$$



22. You start a small baking business, and you want to earn a profit of at least \$250 in the first month. The expenses in the first month are \$155. Write and solve an inequality to represent the possible revenues that you need to earn to meet the profit goal?

$$\begin{array}{r}
 x - 155 \geq 250 \\
 +155 \quad +155 \\
 \hline
 x \geq 405
 \end{array}$$

Need to earn more than \$405

includes

23. Your monthly budget allows you to spend between \$200 and \$450, inclusively. You have already spent \$125. Write and solve a compound inequality to represent how much more money you have to spend for the rest of the month.

$$\begin{array}{r}
 200 \leq x+125 \leq 450 \\
 -125 \quad -125 \quad -125 \\
 \hline
 75 \leq x \leq 325
 \end{array}$$

x = amount of money left to spend

Negative exponents - cross the line
and change the sign

Simplify each.

$$24. x^2 x^{-6} x^0 = x^{2+(-6)+0} = \frac{x^{-4}}{1} = \boxed{\frac{1}{x^4}}$$

$$25. \frac{x^{-8}}{1} = \boxed{\frac{1}{x^8}}$$

$$26. y^{12} y^3 y^1 = y^{12+3+1} = \boxed{y^{16}}$$

$$27. \frac{x^{-1} y^5 x^{-3} x^1 y^2}{1} = x^{-1+(-3)+1} y^{5+2} = \frac{x^{-3}}{1} = \frac{1}{x^3} = \boxed{\frac{y^7}{x^3}}$$

$$28. x^{-7} x^5 = x^{-7+5} = \frac{x^{-2}}{1} = \boxed{\frac{1}{x^2}}$$